## Circumference and Area

| Topic/Skill | Definition/Tips | Example |
| :---: | :---: | :---: |
| 1. Circle | A circle is the locus of all points equidistant from a central point. |  |
| 2. Parts of a Circle | Radius - the distance from the centre of a circle to the edge <br> Diameter - the total distance across the width of a circle through the centre. <br> Circumference - the total distance around the outside of a circle <br> Chord - a straight line whose end points lie on a circle <br> Tangent - a straight line which touches a circle at exactly one point <br> Arc - a part of the circumference of a circle <br> Sector - the region of a circle enclosed by two radii and their intercepted arc Segment - the region bounded by a chord and the arc created by the chord |  |
| 3. Area of a Circle | $\boldsymbol{A}=\boldsymbol{\pi} \boldsymbol{r}^{2}$ which means 'pix radius squared'. | If the radius was 5 cm , then: $A=\pi \times 5^{2}=78.5 \mathrm{~cm}^{2}$ |
| 4. Circumference of a Circle | $\boldsymbol{C}=\boldsymbol{\pi} \boldsymbol{d}$ which means 'pi $\times$ diameter' | If the radius was 5 cm , then: $C=\pi \times 10=31.4 \mathrm{~cm}$ |
| 5. $\pi$ ('pi') | Pi is the circumference of a circle divided by the diameter. $\pi \approx 3.14$ |  |
| 6. Arc Length of a Sector | The arc length is part of the circumference. <br> Take the angle given as a fraction over $360^{\circ}$ and multiply by the circumference. | $\text { Arc Length }=\frac{115}{360} \times \pi \times 8=8.03 \mathrm{~cm}$ |
| 7. Area of a Sector | The area of a sector is part of the total area. <br> Take the angle given as a fraction over $360^{\circ}$ and multiply by the area. | $\text { Area }=\frac{115}{360} \times \pi \times 4^{2}=16.1 \mathrm{~cm}^{2}$ |


| 8. Surface Area of a Cylinder | Curved Surface Area $=\boldsymbol{\pi d h}$ or $\mathbf{2 \pi r h}$ <br> Total SA $=2 \pi r^{2}+\pi d h$ or $2 \pi r^{2}+2 \pi r h$ |  |
| :---: | :---: | :---: |
| 9. Surface Area of a Cone | Curved Surface Area $=\pi r l$ <br> where $l=$ slant height <br> Total SA $=\pi r l+\pi r^{2}$ <br> You may need to use Pythagoras' Theorem to find the slant height |  |
| 10. Surface <br> Area of a Sphere | $S A=4 \pi r^{2}$ <br> Look out for hemispheres - halve the SA of a sphere and add on a circle ( $\pi r^{2}$ ) | Find the surface area of a sphere with radius 3 cm . $S A=4 \pi(3)^{2}=36 \pi \mathrm{~cm}^{2}$ |

Compound area

| Topic/Skill | Definition/Tips | Example |
| :---: | :---: | :---: |
| 1. Metric System | A system of measures based on: <br> - the metre for length <br> - the kilogram for mass <br> - the second for time <br> Length: mm, cm, m, km <br> Mass: $\mathrm{mg}, \mathrm{g}, \mathrm{kg}$ <br> Volume: ml, cl, l | ```1kilometres = 1000 metres 1 \text { metre = 100 centimetres} 1 \text { centimetre = 10 millimetres} 1 kilogram = 1000 grams``` |
| 2. Imperial System | A system of weights and measures originally developed in England, usually based on human quantities <br> Length: inch, foot, yard, miles <br> Mass: lb, ounce, stone <br> Volume: pint, gallon | $1 \mathrm{lb}=16$ ounces <br> 1 foot $=12$ inches <br> 1 gallon $=8$ pints |
| 3. Metric and Imperial Units | Use the unitary method to convert between metric and imperial units. | 5 miles $\approx 8$ kilometres <br> 1 gallon $\approx 4.5$ litres <br> 2.2 pounds $\approx 1$ kilogram <br> 1 inch $=2.5$ centimetres |
| 4. Speed, Distance, Time | Speed = Distance $\div$ Time <br> Distance = Speed x Time <br> Time $=$ Distance $\div$ Speed <br> Remember the correct units. | Speed $=4 \mathrm{mph}$ <br> Time $=2$ hours <br> Find the Distance. $D=S \times T=4 \times 2=8 \text { miles }$ |
| 5. Density, Mass, Volume | Density $=$ Mass $\div$ Volume <br> Mass = Density x Volume <br> Volume $=$ Mass $\div$ Density <br> Remember the correct units. | $\begin{aligned} & \text { Density }=8 \mathrm{~kg} / \mathrm{m}^{3} \\ & \text { Mass }=2000 \mathrm{~g} \end{aligned}$ <br> Find the Volume. $V=M \div D=2 \div 8=0.25 \mathrm{~m}^{3}$ |
| 6. Pressure, Force, Area | Pressure = Force $\div$ Area <br> Force = Pressure x Area <br> Area $=$ Force $\div$ Pressure | $\begin{aligned} & \text { Pressure }=10 \text { Pascals } \\ & \text { Area }=6 \mathrm{~cm}^{2} \end{aligned}$ |


|  |  | Find the Force |
| :--- | :--- | :--- |
|  |  | $F=P \times A=10 \times 6=60 \mathrm{~N}$ |
|  |  |  |

## Drawing, Measuring and Estimating Angles

| 1 | Angle | Where two line segments <br> meet the measure of rotation <br> from one segment to the <br> other. |
| :--- | :--- | :--- |
| 2 | Acute Angle | An angle between $0^{\circ}$ and $90^{\circ}$. |

## Pathway 3

Unit 2 - Drawing, Measuring and Estimating Angles

| 1 |  | Where two line segments meet the measure of rotation from one segment to the other. |  |
| :---: | :---: | :---: | :---: |
| 2 |  | An angle between $0^{\circ}$ and $90^{\circ}$. |  |
| 3 |  | An angle which is exactly $90^{\circ}$. We use a small square to represent a right angle. |  |
| 4 |  | An angle between $90^{\circ}$ and $180^{\circ}$. |  |
| 5 |  | An angle which is greater than $180^{\circ}$. |  |
| 6 |  | The unit that we measure angles in. We use this symbol | $265^{\circ}$ |
| 7 |  | Line segments which meet at right angles |  |
| 8 |  | A mathematical guess. I use my knowledge about angles to estimate the size of an angle. |  |
| 9 |  | The piece of equipment we use to measure angles. |  |

## Pathway 3

Unit 2 - Drawing, Measuring and Estimating Angles


Pathway 3
Unit 2 - Drawing, Measuring and Estimating Angles


Formulae, Sequences and Rules

| 1 | Expression | A mathematical statement <br> written using symbols, numbers <br> or letters. | $6+9$ <br> $5 x+8$ <br> $5 y^{2}$ |
| :--- | :--- | :--- | :---: |
| 2 | Equation | A statement showing that two <br> expressions are equal. | $6+9=15$ <br> $2 y-17=15$ |
| 3 | Formula | An equation linking sets of <br> physical variables. The plural is <br> formulae. | $s=\frac{d}{t}$ |
| 4 | Variable | A letter representing an <br> unknown number. | $5+8=38$ <br> $x$ is the variable |
| 5 | Substitute | Putting a number where a <br> variable is shown. | Example if a $=10$, <br> calculate 4a +2 |
| 6 | Sequence | An ordered set of numbers, <br> shapes or other mathematical <br> objects arranged according to a <br> rule. | Examples: <br> $3,7,11,15,19$ <br> $1,4,9,16,25$ |
| 7 | Arithmetic <br> Sequence / Linear <br> Sequence | A sequence in which terms are <br> generated by adding or <br> subtracting a constant amount <br> each time. | Examples: <br> $1,3,5,7,9,11$ <br> $8,12,16,20,24$ |

Formulae, Sequences and Rules

| 1 |  | A mathematical statement written <br> using symbols, numbers or letters. | $6+9$ <br> $5 x+8$ <br> $5 y^{2}$ |
| :--- | :--- | :--- | :--- |
| 2 |  | A statement showing that two <br> expressions are equal. | $6+9=15$ <br> $2 y-17=15$ |
| 3 |  | An equation linking sets of physical <br> variables. The plural is formulae. | A letter representing an unknown <br> number. |
| 4 |  | Putting a number where a variable is <br> shown. | Example if a = 10, <br> calculate 4a +2 |
| 5 |  | An ordered set of numbers, shapes or <br> other mathematical objects arranged <br> according to a rule. | Examples: <br> $3,7,11,15,19$ <br> $1,4,9,16,25$ |
| 6 |  | A sequence in which terms are <br> generated by adding or subtracting a <br> constant each time. | Examples: <br> 1357911 <br> $8 ~ 12 ~ 16 ~ 20 ~ 24 ~$ |
| 7 |  |  |  |

Formulae, Sequences and Rules

| 1 | Expression |  | $\begin{gathered} 6+9 \\ 5 x+8 \\ 5 y^{2} \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| 2 | Equation |  | $\begin{gathered} 6+9=15 \\ 2 y-17=15 \end{gathered}$ |
| 3 | Formula |  | $s=\frac{d}{t}$ |
| 4 | Variable |  | $5+8=38$ <br> $x$ is the variable |
| 5 | Substitute |  | Example if $\mathrm{a}=10$, calculate $4 a+2$ |
| 6 | Sequence |  | Examples: $\begin{aligned} & 3,7,11,15,19 \\ & 1,4,9,16,25 \\ & \hline \end{aligned}$ |
| 7 | Arithmetic Sequence / Linear Sequence |  | Examples: $1357911$ <br> 812162024 |

Formulae, Sequences and Rules

| 1 |  | A mathematical statement written <br> using symbols, numbers or letters. | $6+9$ <br> $5 x+8$ <br> $5 y^{2}$ |
| :--- | :--- | :--- | :--- |
| 2 |  | A statement showing that two <br> expressions are equal. | $6+9=15$ <br> $2 y-17=15$ |
| 3 |  | An equation linking sets of physical <br> variables. The plural is formulae. | $5=\frac{d}{t}$ |
| 4 | Variable |  | $5+8=38$ <br> Substitute |
| 5 |  | An ordered set of numbers, shapes or <br> other mathematical objects arranged <br> according to a rule. | Examples: <br> $3,7,11,15,19$ <br> $1,4,9,16,25$ |
| 6 |  | A sequence in which terms are <br> generated by adding or subtracting a <br> constant each time. | Examples: <br> 1357911 <br> 8 |
| 7 |  |  |  |

## Fractions

| 1 | Fraction | The result of dividing one integer by a <br> second integer (which must not be zero). It <br> relates parts to a whole. | means <br> one out <br> of three |  |
| :--- | :--- | :--- | :--- | :--- |
| 2 | Vinculum | The fraction line. <br> Denominator | The numerator is the top number in a <br> fraction. <br> The denominator is the bottom number in <br> a fraction. | $\frac{3}{4} \leftarrow_{\text {Nenominator }}$ |

## Introduction to Algebra

| 1 | Expression | A mathematical statement written using symbols, numbers or letters. | $\begin{gathered} 6+9 \\ 5 x+8 \\ 5 y^{2} \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| 2 | Equation | A statement showing that two expressions are equal. | $\begin{gathered} 6+9=15 \\ 2 y-17=15 \end{gathered}$ |
| 3 | Coefficient | A number used to multiply a variable. It can be a letter. | $6 x$ <br> The coefficient is 6 . |
| 4 | $x+1$ | A number plus 1. |  |
| 5 | $x-1$ | A number subtract 1. |  |
| 6 | $1-x$ | Subtract a number from 1. |  |
| 7 | $5 x$ | Multiplying a number by 5. |  |
| 8 | $\frac{x}{4}$ | A number divided by 4. |  |
| 9 | $\frac{4}{x}$ | 4 divided by a number. |  |
| 10 | $x^{2}$ | A number squared. | $x \times x$ |
| 11 | $x^{3}$ | A number cubed. | $x \times x \times x$ |
| 12 | $x y$ | A number multiplied by another number. | $x \times y$ |
| 13 | Simplify Expressions | To write the expression in the simplest way possible. | $\begin{gathered} \text { Simplify } 5 x \times 7 \\ =35 x \end{gathered}$ |
| 14 | Collect Like Terms | The way that you simplify expressions which are added or subtracted. You can only add or subtract terms which have the same letter and power. | Simplify $\begin{aligned} & 2 x+3 y+4 x-5 y \\ & =6 x-2 y \end{aligned}$ |
| 15 | $5(x+3)$ | Five lots of $x+3$. |  |
| 16 | Expand Brackets | Multiply out the brackets. | $5(x+3)=5 x+15$ |
| 17 | $x+x=$ | $2 x$ |  |
| 18 | $7 x+8 x=$ | $15 x$ |  |
| 19 | $7 x-4 x=$ | $3 x$ |  |

## Introduction to Algebra

| 1 |  | A mathematical statement written using symbols, numbers or letters, | $\begin{gathered} 6+9 \\ 5 x+8 \\ 5 y^{2} \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| 2 |  | A statement showing that two expressions are equal. | $\begin{gathered} 6+9=15 \\ 2 y-17=15 \end{gathered}$ |
| 3 |  | The number in front of the letter. | $6 x$ <br> The coefficient is 6 . |
| 4 | $x+1$ |  |  |
| 5 | $x-1$ |  |  |
| 6 | $1-x$ |  |  |
| 7 | $5 x$ |  |  |
| 8 | $\frac{x}{4}$ |  |  |
| 9 | $\frac{4}{x}$ |  |  |
| 10 | $x^{2}$ |  | $x \times x$ |
| 11 | $x^{3}$ |  | $x \times x \times x$ |
| 12 | $x y$ |  | $x \times y$ |
| 13 | Simplify expressions | To write the expression in the most simple way possible. | $\begin{gathered} \text { Simplify } 5 x \times 7 \\ =35 x \end{gathered}$ |
| 14 | Collect like terms | The way that you simplify expressions which are added or subtracted. You can only add or subtract terms which have the same letter and power. | Simplify $\begin{aligned} & 2 x+3 y+4 x-5 y \\ & =6 x-2 y \end{aligned}$ |
| 15 | $5(x+3)$ | Five lots of $x+3$. |  |
| 16 | Expand brackets | Multiply out the brackets. | $5(x+3)=5 x+15$ |
| 17 | $x+x=$ | $2 x$ |  |
| 18 | $7 x+8 x=$ | $15 x$ |  |
| 19 | $7 x-4 x=$ | $3 x$ |  |

## Introduction to Algebra

| 1 |  | A mathematical statement <br> written using symbols, <br> numbers or letters, | $6+9$ |
| :--- | :---: | :--- | :---: |
| 2 |  | A statement showing that two <br> expressions are equal. | $5 x+8$ |
|  |  | The number in front of the <br> letter. |  |
| 3 | $x+1$ |  | $2 y-17=15$ |
| 4 | $x-1$ |  | The coefficient is 6. |

Large and Negative Numbers


Lines and Angles


| 1 |  | Lines that never meet because <br> they are always the same <br> distance from each other. |  |
| :--- | :--- | :--- | :--- |
| 2 |  | Lines that meet at right <br> angles to each other. |  |
| 3 |  | Where two line segments <br> meet the measure of <br> rotation from one segment <br> to the other. | Angles on a straight line <br> sum to 180 |
| 4 |  | Angles around a point sum <br> to 360․ |  |
| 5 |  |  | Vertically opposite angles <br> are equal. |
| 7 |  |  | Interior angles of a triangle <br> sum to 180 |
| 8 |  |  |  |



| 1 |  | Lines that never meet because <br> they are always the same <br> distance from each other. |  |
| :--- | :--- | :--- | :--- |
| 2 |  | Lines that meet at right <br> angles to each other. |  |
| 3 |  | Where two line segments <br> meet the measure of <br> rotation from one segment <br> to the other. |  |
| 5 | Around a Point |  |  |
| 6 | Vertically Opposite |  |  |
| 7 |  |  |  |
| 8 |  |  |  |

Lines and Angles

| 1 | Parallel Lines |  | $\rightarrow$ <br> $>$ |
| :---: | :---: | :---: | :---: |
| 2 | Perpendicular Lines |  |  |
| 3 | Angle |  |  |
| 4 |  | Angles on a straight line sum to $180^{\circ}$. |  |
| 5 |  | Angles around a point sum to $360^{\circ}$. |  |
| 6 |  | Vertically opposite angles are equal. |  |
| 7 | Triangles |  |  |
| 8 | Quadrilaterals |  |  |

Multiplication and Division

| 1 | Product | The result of multiplying two numbers together. | The product of 2 and 3 is 6 because $2 \times 3=6$. |
| :---: | :---: | :---: | :---: |
| 2 | Sum | The result of adding two numbers together. | The sum of 2 and 3 is 5 because $2+3=5$. |
| 3 | Commutative | The order of numbers involved in an operation does not matter and does not affect the answer. <br> Addition and multiplication are commutative. <br> Subtraction and division are not commutative. | $\begin{aligned} & 3+2=2+3 \\ & 4 \times 5=5 \times 4 \\ & 3-2 \neq 2-3 \\ & 10 \div 2 \neq 2 \div 10 \end{aligned}$ |
| 4 | Long Multiplication | When we multiply two large numbers together we can use the long multiplication method. |  |
| 5 | Dividend | The number that is being divided. | dividend $\div$ divisor $=$ quotient$30 \div 6=5$ |
| 6 | Divisor | The number by which another is divided. |  |
| 7 | Quotient | The result of a division. |  |
| 8 | Short Division | A written method of dividing. |  |
| 9 | Grid Method | This method is used for multiplication. It involves partitioning numbers into hundreds, tens and units before they are multiplied. | $35 \times 7$ |
|  |  |  | $\times \quad 30 \quad 5$ |
|  |  |  | 7 210 35 |
|  |  |  | $\mathbf{2 1 0}+\mathbf{3 5}=\mathbf{2 4 5}$ |
| 10 | Column Method | This method of multiplication, addition and subtraction is the method where numbers are 'carried' or 'borrowed'. | The column method for multiplication the carried numbers can go above or below. $\begin{array}{r} 237 \\ \times \quad 4 \\ \hline 948 \end{array}$ |

## Pathway 4

Unit 2 - Multiplication and Division

| 1 |  | The result of multiplying two numbers together. | The product of 2 and 3 is 6 because $2 \times 3=$ 6. |
| :---: | :---: | :---: | :---: |
| 2 |  | The result of adding two numbers together. | The sum of 2 and 3 is 5 because $2+3=$ 5. |
| 3 | Commutative |  | $\begin{aligned} & 4 \times 7=7 \times 4 \\ & 4+7=7+4 \end{aligned}$ |
| 4 | Long Multiplication | When we multiply two large numbers together we can use the long multiplication method. | $\begin{array}{r} 7232 \\ 16 \mathrm{X} \\ \hline 43392 \\ 447 \\ 72320 \\ \hline 115712 \end{array}$ |
| 5 |  | The number that is being divided. | $\begin{gathered} 30 \div 16=5 \\ \text { dividend } \div \text { divisor }=\text { quotient } \end{gathered}$ |
| 6 | Divisor |  |  |
| 7 |  | The result of a division |  |
| 8 | Short division | A written method of dividing. | $186+6=\begin{array}{llll} 0 & 3 & 1 \\ 6 & 1^{1} 8 & 6 \end{array}$ |

## Pathway 4

Unit 2 - Multiplication and Division
\(\left.\left.$$
\begin{array}{|l|l|l|l|}\hline 1 & \text { Product } & & \begin{array}{l}\text { The product of } \\
2 \text { and 3 is 6 } \\
\text { because 2 x 3 }\end{array} \\
6 .\end{array}
$$\right] \begin{array}{l}The sum of 2 <br>
and 3 is 5 <br>
because 2 + 3 = <br>

5 .\end{array}\right]\)| $4 \times 7=7 \times 4$ |
| :--- |
| 2 |



## Pathway 4

Unit 2 - Multiplication and Division

| 1 |  |  |  |
| :--- | :--- | :--- | :--- |
| 2 |  |  |  |
| 3 |  |  |  |
| 4 |  |  |  |
| 5 |  |  |  |
| 6 |  |  |  |
| 7 |  |  |  |
| 8 |  |  |  |

Percentages

| 1 | Percentage | A percentage is a fraction expressed as <br> the number of parts per hundred. It is <br> recorded using the notation $\%$ | $89 \%$ <br> $105 \%$ <br> $0.67 \%$ |
| :--- | :--- | :--- | :---: |
| 2 | Vinculum | The fraction line. | $\frac{3}{4}$ |
| 3 | Write an amount <br> as a percentage of <br> another | Write as a fraction and multiply by 100. | $\frac{14}{17} \times 100=82.4 \%$ (1dp) |

## Pathway 6

Unit 4 - Percentages
MEA


## Pathway 6

Unit 4 - Percentages
MEA

| 1 | Percentage |  | $\begin{gathered} 89 \% \\ 105 \% \\ 0.67 \% \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| 2 | Vinculum |  | $\frac{3}{4}$ |
| 3 | Write an amount as a percentage of another |  | $\frac{14}{17} \times 100=82.4 \%_{(1 d p)}$ |
| 4 | Find $10 \%$ of an amount |  | $56 \div 10=5.6$ |
| 5 | Find 1\% of an amount |  | $56 \div 100=0.56$ |
| 6 | Find $5 \%$ of an amount |  | $(56 \div 10) \div 2=2.8$ |
| 7 | Find 20\% of an amount |  | $(56 \div 10) \times 2=11.2$ |
| 8 | Percentage <br> Multiplier |  | Find $57 \%$ of 893 $893 \times 0.57=509.01$ |
| 9 | Percentage Increase/Decrease |  | Increase 500 by $20 \%$ (N-Calc) <br> $10 \%$ of $500=50$ <br> so $20 \%$ of $500=100$ $500+100=600$ <br> Decrease 800 by $17 \%$ (Calc): $100 \%-17 \%=83 \%$ $83 \% \div 100=0.83$ |
| 10 | Percentage Change |  | $\frac{\text { new value }- \text { original value }}{\text { orginal value }} \times 100$ |
| 11 | 0.5 |  | 50\% |
| 12 | 0.25 |  | 25\% |
| 13 | 0.75 |  | 75\% |
| 14 | 0.2 |  | 20\% |
| 15 | 0.125 |  | 12.5\% |
| 16 | 0.7 |  | 70\% |
| 17 | $0 . \dot{3}$ |  | $33.3 \%_{(1 \mathrm{dp})}$ |

Pathway 6
Unit 4 - Percentages


Topic: Perimeter and Area

| Topic/Skill | Definition/Tips | Example |
| :--- | :--- | :--- | :--- |
| 1. Perimeter |  |  |
| Shape. |  |  |
| Units include: $\mathrm{mm}, \mathrm{cm}, \mathrm{m}$ etc. |  |  |$\quad$| The amount of space inside a shape. |
| :--- |
| Units include: $\mathrm{mm}^{2}, \mathrm{~cm}^{2}, \mathrm{~m}^{2}$ |

## Place Value

| 1 | Integer | A whole number. It can be negative or positive. | $-7,4,0,2,19,897$ |
| :---: | :---: | :---: | :---: |
| 2 | Decimal | A number with a decimal point in it. It can be positive or negative. | $\begin{aligned} & 4.5 \\ & -4.5 \end{aligned}$ |
| 3 | Place Value | The value of a digit that relates to its position or place in a number. | 5300 <br> The value of the 3 is 300 |
| 4 | Digits | The symbols we use to write a number. | 456 has 3 digits |
| 5 | Place Value Columns | The names of the columns tell us the value of the digits. |  |
| 6 | Ordering | Putting a list of numbers in order. Ascending is from smallest to greatest. <br> Descending is from greatest to smallest. | Ascending order: $7,13,45,78,124$ <br> Descending order: $567,67,42,16,3$ |
| 7 | Partitioning | Splitting a number up. | $\stackrel{\downarrow}{100} \stackrel{1}{156} \downarrow_{6}$ |
| 9 | Reading <br> Large <br> Numbers | Start at the decimal point and work your way left along the place value chart to find the value of each digit up to 1,000 . | $1,256$ <br> One thousand, two hundred and fifty six. |
| 10 | Comparing Numbers | We use these symbols <br> = Equal to <br> < Less than <br> $>$ Greater than <br> $\geq$ Greater than or equal to <br> $\leq$ Less than or equal to | $3<6$ <br> 3 is less than 6 $6>3$ <br> 6 is greater than 3 |
| 11 | Positive numbers | Numbers that are greater than zero. | 5 is positive 5. |
| 12 | Negative Numbers | Numbers that are less than zero. | - 5 is negative 5. |
| 13 | Rounding | To change a number to a similar number which is either easier to read or easier to calculate with. <br> If the digit to the right of the rounding digit is less than 5 , round down. | 74 rounded to the nearest ten is 70 , because 74 is closer to 70 than 80 . |


| Topic/Skill | Definition/Tips | Example | Your Turn |
| :---: | :---: | :---: | :---: |
| Probability | The likelihood/chance of something happening. <br> Is expressed as a fraction, decimal, percentage between 0 (impossible) and 1 (certain). |  | The chance of flipping a coin and getting heads is: <br> The chance of flipping a coin and it flying into space is: |
| Sample | A sample is a small selection of items from a population. <br> A sample is biased if individuals or groups from the population are not represented in the sample. | A sample could be selecting 10 students from a year group at school. | I want to know about the favourite subjects of all pupils in our school. I conduct a survey asking girls in Year 11. What is wrong with my sample? |
| Sample <br> Size | The larger a sample size, the closer those probabilities will be to the true probability. | A sample size of 100 gives a more reliable result than a sample size of 10. | Why don't survey's just ask everyone in the population? |
| Theoretical Probability | $\frac{\text { Number of Favourable Outcomes }}{\text { Total Number of Possible Outcomes }}$ | Probability of rolling a 4 on a fair 6 sided die $=\frac{1}{6}$ | The probability of rolling an even number on a fair 6 -sided dice is: |
| Relative Frequency | $\frac{\text { Number of Successful Trials }}{\text { Total Number of Trials }}$ | A coin is flipped 50 times and lands on Tails 29 times. <br> The relative frequency of getting $\text { Tails }=\frac{29}{50} \text {. }$ | A dice is rolled 100 times and lands on 314 times. <br> The relative frequency of getting $3=$ |


| Exhaustive | Outcomes are exhaustive if they cover the entire range of possible outcomes. <br> The probabilities of an exhaustive set of outcomes adds up to 1 . | When rolling a six-sided die, the outcomes 1, 2, 3, 4, 5 and 6 are exhaustive, because they cover all the possible outcomes. $\frac{1}{6}+\frac{1}{6}+\frac{1}{6}+\frac{1}{6}+\frac{1}{6}+\frac{1}{6}=\frac{6}{6}=1$ | When flipping a coin... |
| :---: | :---: | :---: | :---: |
| Mutually Exclusive | Events are mutually exclusive if they cannot happen at the same time. <br> The probabilities of an exhaustive set of mutually exclusive events adds up to 1 . | Examples of mutually exclusive events: <br> - Turning left and right <br> - Heads and Tails on a coin <br> Examples of non mutually exclusive events: <br> - King and Hearts from a deck of cards, because you can pick the King of Hearts | Put a tick or a cross for mutally exclusive ( $\checkmark$ ) and non mutually exclusive ( $\mathbf{X}$ ) events: Choosing a random pupil in a high school survey: <br> - Getting someone with glasses or someone without glasses <br> - Getting someone in Year 10 or in Year 11 <br> - Getting a boy in Year 7 or a girl in Year 7 |
| Independent Events | The outcome of a previous event does not influence/affect the outcome of a second event. | An example of independent events could be being late to school and eating a jacket potato for lunch | Tick the correct example: <br> - Being in Year 7 and being in KS3 <br> - Being a boy and liking maths |
| Dependent Events | The outcome of a previous event does influence/affect the outcome of a second event. | An example of dependent events could be being late to school and missing the train | Tick the correct example: <br> - Flipping a coin and getting heads, and then flipping and getting heads again <br> - Pulling a green marble out of a bag and then pulling another green marble |


| Expected Outcomes | To find the number of expected outcomes, multiply the probability by the number of trials. | The probability that a football team wins is 0.2 How many games would you expect them to win out of 40 ? $0.2 \times 40=8 \text { games }$ | I roll a fair 6-sided dice 300 times. How many times would you expect to get a 5 ? |
| :---: | :---: | :---: | :---: |
| Probability Notation | $P(A)$ refers to the probability that event A will occur. <br> $P\left(A^{\prime}\right)$ refers to the probability that event A will not occur. <br> $P(A \cup B)$ refers to the probability that event $A$ or $B$ or both will occur. <br> $P(A \cap B)$ refers to the probability that both events $A$ and $B$ will occur. | P(Red Queen) refers to the probability of picking a Red Queen from a pack of cards. <br> P(Blue') refers to the probability that you do not pick Blue. <br> P(Blonde $\cup$ Right Handed) refers to the probability that you pick someone who is Blonde or Right Handed or both. <br> P(Blonde $\cap$ Right Handed) refers to the probability that you pick someone who is both Blonde and Right Handed. | All these are for fair 6-sided dice: $\begin{aligned} & P(6) \text { refers to... } \\ & P(1 \cup 6) \ldots \\ & P\left(5^{\prime}\right) \ldots \\ & P(3 \cap 4) \ldots \end{aligned}$ |
| AND rule for Probability | When two events, $A$ and $B$, are independent: $P(A \text { and } B)=P(A) \times P(B)$ | What is the probability of rolling a 4 and flipping a Tails? $\begin{gathered} P(4 \text { and Tails })=P(4) \times P(\text { Tails }) \\ =\frac{1}{6} \times \frac{1}{2}=\frac{1}{12} \end{gathered}$ | What is the probability of rolling a 3 and flipping a Heads? |


| OR rule for Probability | When two events, $A$ and $B$, are mutually exclusive: $P(A \text { or } B)=P(A)+P(B)$ | What is the probability of rolling a 2 or rolling a 5 ?$\begin{gathered} P(2 \text { or } 5)=P(2)+P(5) \\ =\frac{1}{6}+\frac{1}{6}=\frac{2}{6}=\frac{1}{3} \end{gathered}$ |  |  |  |  |  |  | What is the probability of flipping and getting a Heads or a Tails? |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency Tree | A diagram showing how information is categorised into various categories. <br> The numbers at the ends of branches tells us how often something happened (frequency). <br> You can work out the missing numbers by making sure they add up. |  |  |  |  |  |  |  |  |  |  |  |
| Sample Space | The set of all possible outcomes of an experiment. <br> For example, the diagram shows all the different possible outcomes of rolling two dice and adding the scores. |  | 1 | 2 | 3 | 4 | 5 | 6 | Spinner 2 | $\times$ | Spinner 1 |  |
|  |  |  | 2 | 3 | 4 | 5 | 6 | 7 |  |  | 2 | 3 |
|  |  |  | 3 | 4 | 5 | 6 | 7 | 8 |  |  |  |  |
|  |  |  | 4 | 5 | 6 | 7 | 8 | 9 |  |  |  |  |
|  |  |  | 5 | 6 | 7 | 8 | 9 | 10 |  | 3 |  |  |
|  |  |  | 6 | 7 | 8 | 9 | 10 | 11 |  |  |  |  |
|  |  |  | 7 | 8 | 9 | 10 | 11 | 12 |  |  |  |  |


| Tree Diagrams | Tree diagrams show all the possible outcomes of an event and calculate their probabilities. <br> All branches must add up to 1 when adding downwards. <br> This is because the probability of something not happening is 1 minus the probability that it does happen. They are exhaustive. <br> Multiply going across a tree diagram to work out the probability of both events happening. <br> Fractions or decimals, the process is the same | The probability of getting a Black from Bag A and a Red from Bag B is $\frac{4}{5} \times \frac{1}{3}=\frac{4}{15}$ | James goes to an arcade. He has one go on the Teddy Grabber. He has one go on the Penny Drop. The probability that he wins on the Teddy Grabber is 0.2 . The probability that he wins on the Penny Drop is 0.3 . <br> Find the probability that he wins both games: |
| :---: | :---: | :---: | :---: |
| Conditional Probability | The probability of an event A happening, given that event $B$ has already happened. <br> With conditional probability, check if the numbers on the second branches of a tree diagram changes. For example, if you have 4 red beads in a bag of 9 beads and pick a red bead on the first pick, then there will be 3 red beads left out of 8 beads on the second pick. |  | Draw a tree diagram for a bag with 5 red marbles and 5 yellow marbles, with two counters picked: |


| Venn Diagrams | A Venn Diagram shows the relationship between a group of different things and how they overlap. <br> You may be asked to shade Venn Diagrams as shown below and to the right. <br> The Union <br> The Intersection <br> 'A or B or Both' <br> 'A intersection | $(A \cap B)^{\prime}$ <br> $(A \cup B)$ |  |
| :---: | :---: | :---: | :---: |
| Venn Diagram Notation | $\in$ means 'element of a set' (a value in the set) <br> \{ \} means the collection of values in the set. <br> $\xi$ means the 'universal set' (all the values to consider in the question) <br> A' means 'not in set A' (called complement) <br> $A \cup B$ means ' $A$ or $B$ or both' (called Union) <br> $A \cap B$ means ' $A$ and $B$ (called Intersection) | Set $A$ is the even numbers less than 10. $A=\{2,4,6,8\}$ <br> Set $B$ is the prime numbers less than 10 . $B=\{2,3,5,7\}$ <br> $A \cup B=\{2,3,4,5,6,7,8\}$ <br> $A \cap B=\{2\}$ | Set $A$ is the odd numbers less than 15. $A=$ <br> Set $B$ is the square numbers less than 30. $B=$ <br> $A \cup B=$ <br> $A \cap B=$ <br> $A^{\prime} \cap B=$ |

## Properties of Shapes

| 1 | 2 D | Two-dimensional. <br> Describes a plane (flat) shape with <br> a length and width. | Examples of 2D shapes <br> include: <br> triangle, square, pentagon |
| :--- | :--- | :--- | :--- |
| 2 | 3 D | Three-dimensional <br> Describes a solid shape with a <br> length, width and depth. | Examples of 3D shapes <br> include a: cube, sphere, <br> prism |
| 3 | Polygon | A plane shape with three or more <br> straight sides. |  |
| 4 | Triangle | A polygon with three sides. <br> Right- <br> Tangle <br> Triangle | A triangle with one internal right- <br> angle. |
| 6 | Tquilateral <br> Triangle | A triangle which has three equal <br> length sides and internal angles <br> which measure $60^{\circ}$. |  |
| 7 | Isosceles <br> Triangle | A triangle which has two sides of <br> equal length and equal sized base <br> angles. |  |
| 10 | Scalene <br> Triangle | A triangle where the three sides <br> are of different length. |  |
| 9 | Square | A polygon with four equal length <br> sides and four internal right <br> angles. |  |
| 10 | A polygon with two pairs of <br> opposite equal length sides and <br> four internal right angles |  |  |

## Ratio

| 1 | Proportion | A part to whole comparison. <br> Any two variables are directly proportional if they are related in the same ratio by a multiplier in the form $y=k x$. | $£ 20$ is shared between two people in the ratio $3: 5$, the first person received $3 / 8$ of the whole. This is their proportion of the whole. <br> In currency exchange the ratio $£ 1$ : $€ 1.20$ shows that pounds are directly proportional to euros. £1 = 1.2 x Euros |
| :---: | :---: | :---: | :---: |
| 2 | Ratio | Ratio compares the size of one part to another part. | The order is important, the ratio of $a$ to $b$ is written $a: b$ |
| 3 | Unitary ratio | A part to part comparison where one part is 1. <br> It is written as $1: \mathrm{n}$ or $\mathrm{n}: 1$ |  |
| 4 | Fraction | Any part of a group, number or whole. <br> The numerator tells us how many parts we have. <br> The denominator tells us how many parts the whole has been split into. | $\frac{\text { Numerator }}{\text { Denominator }}$ |
| 5 | Respectively | One after the other in the order already mentioned. |  |

## Representing Data

$\left.\begin{array}{|l|l|l|l|}\hline 1 & \text { Data } & \begin{array}{l}\text { A collection of information. Usually } \\ \text { gathered by observation, } \\ \text { questioning or measurement. }\end{array} & \begin{array}{l}\text { There are two types of data: } \\ \text { Continuous data can have an infinite } \\ \text { number of possible values within a } \\ \text { selected range. For example, height } \\ 158.5 \mathrm{~cm}, 142.028 \mathrm{~cm}, 180.1 \mathrm{~cm} .\end{array} \\ \text { Discrete data only has a limited number } \\ \text { of possible values. For example, shoe } \\ \text { size } 5,51 / 2,6,61 / 2,7 \text { etc. }\end{array}\right\}$

Unit 8 - Representing Data

| 1 |  | A collection of information. Usually <br> gathered by observation, <br> questioning or measurement. | There are two types of data: <br> Continuous data can have an infinite <br> number of possible values within a <br> selected range. For example, height <br> $158.5 \mathrm{~cm}, 142.028 \mathrm{~cm}, 180.1 \mathrm{~cm}$. <br> Discrete data only has a limited number <br> of possible values. For example, shoe <br> size 5, 512, 6, 612, 7 etc. |
| :--- | :--- | :--- | :--- |
| 2 |  | The number of times a particular <br> item appears in a set of data. | In maths we have frequency tables <br> which show the number of items in a <br> data set. |
| 3 |  | From the Old French interpreter <br> which meant "explain or translate". <br> It means to expound the meaning, <br> render clear or explicit. | To interpret data using graphs means to <br> find meaning from the graph and to <br> understand what it is telling us. |
| 4 |  | From the Old French representer <br> "present, show or display". It means <br> to symbolise, to serve as a sign. | To represent data is to make it present <br> and show what it means. This means to <br> turn 'raw' data into a graph. |
| 5 |  | There are many types of graph. <br> Examples include bar graph, pie <br> chart and pictogram. | ( |

## Pathway 5

Unit 8 - Representing Data

| 1 | Data |  | There are two types of data: <br> Continuous data can have an infinite number of possible values within a selected range. For example, height $158.5 \mathrm{~cm}, 142.028 \mathrm{~cm}, 180.1 \mathrm{~cm}$. <br> Discrete data only has a limited number of possible values. For example, shoe size $5,51 / 2,6,6112,7$ etc. |
| :---: | :---: | :---: | :---: |
| 2 | Frequency |  | In maths we have frequency tables which show the number of items in a data set. |
| 3 | Interpreting |  | To interpret data using graphs means to find meaning from the graph and to understand what it is telling us. |
| 4 | Represent |  | To represent data is to make it present and show what it means. This means to turn 'raw' data into a graph. |
| 5 | Types of Graph |  |  |

Unit 8 - Representing Data

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| :--- | :--- | :--- | :--- |
| 2 |  | The number of times a particular <br> item appears in a set of data. | In maths we have frequency tables <br> which show the number of items in a <br> data set. |
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| 5 | Types of Graph |  |  |

## Rounding and Arithmetic

| 1 | Rounding | To change a number to a similar number which is either easier to read or easier to calculate with. <br> If the digit to the right of the rounding digit is less than 5 , round down. | We can round to a number of decimal places or significant figures, to the nearest 10,100 or 1000 , or to the nearest integer. |
| :---: | :---: | :---: | :---: |
| 2 | Upper Boundary | The highest that a number could have been before it was rounded. |  |
| 3 | Lower Boundary | The lowest that a number could have been before it was rounded. |  |
| 4 | Distributive Law | The Distributive Law states that multiplying a number by a group of numbers added together is the same as doing each multiplication separately. | $12 \times 3$ is the same as $(10 \times 3)+(2 \times 3)$ or $(8 \times 3)+(4 \times 3)$ |
| 5 | Commutative Law | The Commutative Law states that the answer of any sum or product is unchanged by re-ordering the calculation. <br> Addition and multiplication are commutative. | $\begin{aligned} & 3 \times 4=4 \times 3 \\ & 3+4=4+3 \end{aligned}$ |
| 6 | Grid Method | This method is used for multiplication. It involves partitioning numbers into hundreds, tens and units before they are multiplied. | $35 \times 7$$\times$ 30 5 <br> 7 210 35$210+35=245$ |
| 7 | Column Method | This method of multiplication, addition and subtraction is the method where numbers are 'carried' or 'borrowed'. | The column method for multiplication the carried numbers can go above or below. |

## Pathway 2

Unit 4 - Rounding and arithmetic



## The Probability Scale

| 1 | Probability | The likelihood of an event happening. <br> It can be expressed in words or in numbers <br> on a scale from 0 to 1. <br> We write probabilities as fractions, <br> decimals or percentages. |  |
| :--- | :--- | :--- | :--- |
| 2 | Impossible | The probability is 0. | It is impossible to roll a 7 <br> on a normal die. |
| 3 | Certain | Even Chance | The probability is 1. <br> Also called fifty-fifty chance or evens. |
| 4 | Total Probability | It is certain that you will <br> roll a number between 1- <br> 6 on a normal die. |  |
| 5 | All the probabilities of an event, where <br> of getting tails when <br> flipping a coin. |  |  |
| 6 | Outcome | The result of a single trial of an experiment. |  |
| 7 | Mutually Exclusive | Events are mutually exclusive if it is <br> impossible for them to both happen at the <br> same time. | Flipping a heads or tails <br> on a coin is mutually <br> exclusive. You cannot get <br> both at the same time. |



Time

| 1 | Quarter-past | It is fifteen minutes past the hour. <br> The minute hand is pointing to the 3 . | Quarter-past Eight Eight Fifteen 8:15 |
| :---: | :---: | :---: | :---: |
| 2 | Quarter-to | It is 15 minutes until the next hour. <br> The minute hand is pointing to the 9 . | Quarter-to Ten Nine Forty-five 9:45 |
| 3 | Five-past, Ten-past, <br> Twenty-past, Twenty-five-past' | It is this many minutes past the hour. |  |
| 4 | Five-to, Ten-to, Twenty-to, Twenty-five-to | It is this many minutes until the next hour. |  |
| 5 | Analogue Clock | A clock that usually has 12 divisions labelled 1 to 12 to represent the hours. <br> The long hand is the minute hand. The shorter hand is the hour hand. |  |
| 6 | Digital Clock | A clock that shows the time in digits. | $4: 36$ |
| 7 | Day | A unit of time. <br> There are 365 days in a year. |  |
| 8 | Week | A unit of time. <br> There are 52 weeks in a year. |  |
| 9 | Hour | A unit of time. <br> There are 24 hours in one day. |  |
| 10 | Minute | A unit of time. <br> There are 60 minutes in one hour. |  |
| 11 | Second | A unit of time. <br> There are 60 seconds in one minute. |  |
| 12 | AM | AM indicates the morning (before 12 midday). It comes from the Latin for 'before midday'. | 6AM is six o'clock in the morning. |
| 13 | PM | The afternoon and evening. It comes from the Latin for 'after midday'. | 6PM is six o'clock in the evening. |
| 14 | 24 Hour Clock | The time is given in the number of hours and minutes since midnight. | 13: 15 means $1: 15 \mathrm{pm}$ |

Times Tables and Formal Methods for Addition and Subtraction

| 1 | Multiplication | The operation where a number is added to itself a number of times to form a product. | Synonyms: <br> 'times', 'multiply', <br> 'repeated addition', <br> 'product’, 'lots of' and 'groups of'. |
| :---: | :---: | :---: | :---: |
| 2 | Division | The operation where a number is shared or grouped into a number of equal parts. | Synonyms: 'divide', 'share equally' and 'divided by'. |
| 3 | Addition | The operation to combine numbers or quantities to form a total or sum. Addition is the inverse of subtraction. | Synonyms: <br> 'sum', 'add', 'plus', 'more', 'total' and 'all together'. |
| 4 | Subtraction | The operation to find the difference between two numbers of quantities. Subtraction is the inverse of addition. | Synonyms: <br> 'minus', 'take away', 'subtract', 'reduce', 'take from', 'difference', 'decrease', 'fewer', and 'between'. |
| 5 | Inverse Operations | The opposite operation. Inverse operations 'undo' each other. | Addition and Subtraction. Multiplication and Division. |
| 6 | Column Method | Lining up numbers and performing an operation using a formal algorithm. | $\begin{array}{r} 52 \\ +\quad 64 \end{array}$ |
| 7 | Commutative | The order of numbers involved in an operation does not matter and does not affect the answer. <br> Addition and multiplication are commutative. <br> Subtraction and division are not commutative. | $\begin{aligned} & 3+2=\angle+3 \\ & 4 \times 5=5 \times 4 \\ & \\ & 3-2 \neq 2-3 \\ & 10 \div 2 \neq 2 \div 10 \end{aligned}$ |

